

# **Shiftk Documentation**

Release 2.0.0

kawamura

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#### **OVERVIEW**

This is document for the sample program which uses K  $\omega$  library in the ISSP Math Library; this program computes the Green 's function with  $K\omega$ . For the details of K  $\omega$  library, See " $K\omega$  manual" in this package.

# 1.1 Calculation in this program

This program compute the Green 's function

$$G_i(z) = \langle i | (z - \hat{H})^{-1} | i \rangle \equiv \varphi_i^* \cdot (z - \hat{H})^{-1} \varphi_i, \qquad (1.1)$$

where  $|i\rangle$  is a wavefunction,  $\mathcal{H}$  is the Hamiltonian, and z is a complex frequency.

 $\mathcal{H}$  in the above equation is obtained by either the following two ways:

- Input  ${\mathcal H}$  as a file with the MatrixMarket format
- Construct  $\mathcal{H}$  as a Hamiltonian of the Heisenberg model in this program.

In the computation of the Green 's function, we use either the following two method according to the type of  $\hat{H}$  (a real- or a complex- number).

- $\hat{H}$  of real numbers : Shifted Bi-Conjugate Gradient(BiCG) method
- $\hat{H}$  of complex numbers : Shifted Conjugate Orthogonal Conjugate Gradient(COCG) method

## TWO

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# THREE

# PREREQUISITE

- fortran compiler
- K  $\omega$  library
- BLAS, LAPACK
- MPI library (Optional)

## **OVERALL PROCEDURE**

This program performs simulation as follows (See Fig. 1):

- 1. Read a input file for the numerical condition.
- 2. (Optional) Read input files for the Hamiltonian and the right hand side vector.
- 3. (Optional) Read a file for the restart ( $\alpha$ ,  $\beta$ , residual vectors)
- 4. (Bi)CG iteration with  $K\omega$  library
- 5. Output results (Green 's function, residual vectors,  $\alpha$ ,  $\beta$ )

We introduce the detailed procedure as follows. The format of each file is written in Format of files.

## 4.1 Calculation from scratch

#### 4.1.1 Prepare input file

In this input file, we specify the frequency grid, the maximum number of iteration, etc.

A example of this input file is shown as follow.

```
&filename
 inham = ""
  invec = ""
&ham
nsite = 4
Jx = 1d0
Jy = 1d0
Jz = 1d0
Dz = 0d0
&cg
 maxloops = 100
  convfactor = 6
&dyn
 calctype = "normal"
 nomega = 100
  omegamin = (-2d0, 0.1d0)
  omegamax = (1d0, 0.1d0)
  outrestart = .TRUE.
```

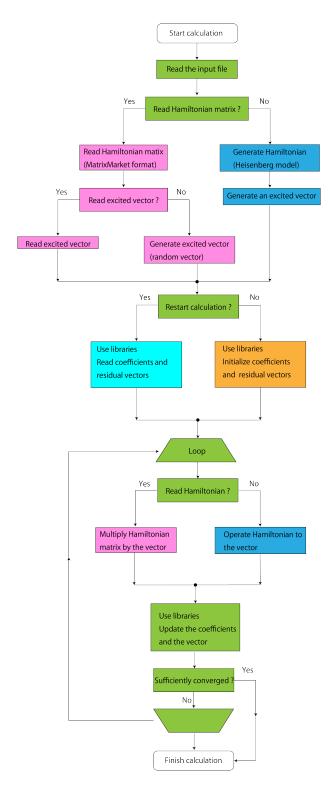


Fig. 1: Figure 4: Schematic flow of the calculation of this program.

where InHam is the file-name for the Hamiltonian in the MatrixMarket format, InVec is the file-name of the right hand side vector, NOmega is the number of frequencies where the dynamical Green's function is computed. OmegaMin is the lower limit of the frequency z, OmegaMax is the upper limit of the frequency z. These complex frequencies must be written as "({Real part}, {Imaginaly part})". The frequency grid is defined as

$$\omega_n = \texttt{OmegaMin} + \frac{n-1}{\texttt{NOmega} - 1}(\texttt{OmegaMax} - \texttt{OmegaMin}). \tag{4.1}$$

MaxLoops is the maximum number of iterations. For the details of this input file, see "*Namelist*" *file*. The string variable must be specified with two ' or ".

#### 4.1.2 (Optional) Prepare input file for the Hamiltonian and RHS vector

Prepare input files for the Hamiltonian (MatrixMarket format) and right hand side vector.

An example of the file of the right hand side vector is shown as follows:

```
256
0.01 0.0
0.05 0.0
0.1 0.0
(continue ...)
```

Details of the file format is written in "InHam" file and "InVec" file.

#### 4.1.3 Launch

Execute a program ShiftK.out with a namelist file namelist.def as follows:

```
$ ShiftK.out namelist.def
```

#### 4.1.4 Output

The following files are generated in output/ directory (this directory is also generated by this program).

TriDiagComp.dat, ResVec.dat, dynamicalG.dat

where TriDiagComp.dat contains the parameters for the restart, ResVec.dat contains the residual vector, dynamicalG.dat contains the dynamical Green's function. The format of these file is written in *Residual vector* - *Dynamical Green's function*.

## 4.2 Catch up

Compute the Green's function at the different frequency by using the information of output/TriDiagComp.dat that are generated in the previous run. This calculation does not require the matrix-vector product.

#### 4.2.1 Modify the namelist file

Change calctype parameter in the file namelist.def from "normal" to "recalc". OmegaMin, OmegaMax, etc. can be modified.

#### 4.2.2 Launch

Execute a program ShiftK.out with a namelist file namelist.def as follows:

```
$ ShiftK.out namelist.def
```

The output/dynamicalG.dat will be overwritten.

#### 4.2.3 Output

The same output files as the previous section are generated.

## 4.3 Restart

Compute the Green's function at the different frequency by using the information of output/TriDiagComp.dat and output/ResVec.dat that are generated in the previous run.

#### 4.3.1 Modify the namelist file

Change calctype parameter in the file namelist.def from "normal" to "restart". OmegaMin, OmegaMax, etc. can be modified. Parameters InHam, InVec, and the files of the Hamiltonian and RHS vector can not be modified.

#### 4.3.2 Launch

Execute a program ShiftK.out with a namelist file namelist.def as follows:

\$ ShiftK.out namelist.def

The output/dynamicalG.dat will be overwritten.

#### 4.3.3 Output

The following files are generated (or are overwritten) in output / directory.

```
TriDiagComp.dat, ResVec.dat, dynamicalG.dat
```

where TriDiagComp.dat contains the parameters for the restart, ResVec.dat contains the residual vector, dynamicalG.dat contains the dynamical Green's function. The format of these file is written in *Residual vector* - *Dynamical Green's function*.

## FORMAT OF FILES

## 5.1 Input files

## 5.1.1 "Namelist" file

This file has four namelist (filename, ham, cg, dyn). For the details of the namelist of fortran, see some books and Web page for fortran.

```
&filename
 inham = ""
  invec = ""
/
&ham
nsite = 4
Jx = 1d0
Jy = 1d0
Jz = 1d0
Dz = 0d0
/
&cg
 maxloops = 100
 convfactor = 6
&dyn
 calctype = "normal"
 nomega = 100
  omegamin = (-2d0, 0.1d0)
  omegamax = (1d0, 0.1d0)
  outrestart = .TRUE.
```

In the namelist "filename", we specify the file names of the Hamiltonian and the RHS vector.

• InHam

Type : string (default: "")

**Description :** The name of the file for the Hamiltonian in the MatrixMarket format (full path or relative path). If this parameter is not specified, the Hamiltonian of the 1D spin chain is generated with the parameters in ham namelist.

• InVec

Type : string (default: "")

**Description :** The name of the file for the right hand side vector. If this parameter is not specified, the RHS vector is generated as follows: First the ground-state vector is computed. Then RHS vector is calculated by operating  $\hat{S}_{1z}$  (*z* component of the spin at site 1) to the ground-state vector. Therefore, we assume the computed system is the one-dimensional spin chain.

"ham" namelist is read only when InHam is not specified. The parameters in this namelist are used to generate the Hamiltonian of the one-dimensional spin chain (See Fig. 1)

$$\hat{H} = \sum_{i} \begin{pmatrix} \hat{S}_{ix} & \hat{S}_{iy} & \hat{S}_{iz} \end{pmatrix} \begin{pmatrix} J_x & D_z & 0\\ -D_z & J_y & 0\\ 0 & 0 & J_z \end{pmatrix} \begin{pmatrix} \hat{S}_{i+1x} & \hat{S}_{i+1y} & \hat{S}_{i+1z} \end{pmatrix}.$$
(5.1)

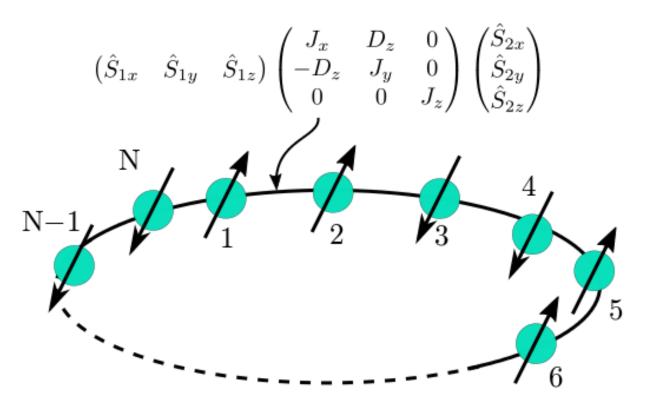


Fig. 1: Figure 2: Schematic picture of the one-dimensional spin chain.

• nsite

**Type :** int (default: 4)

Description : The number of sites in the 1D spin chain model.

• Jx

**Type :** double (default: 1.0)

**Description :**  $J_x$  for the Heisenberg model.

• Jy

**Type :** double (default: 1.0)

**Description :**  $J_y$  for the Heisenberg model.

• Jz

**Type :** double (default: 1.0)

**Description :**  $J_z$  for the Heisenberg model.

• Dz

**Type :** double (default: 0.0)

**Description :** The parameter of the Dzyaloshinskii-Moriya interaction  $(D_z)$ .

og namelist has parameters for specifying the numerical condition for the (Bi)Conjugate-gradient method.

• MaxLoops

Type : int (default: the dimension of the Hamiltonian)

**Description :** The maximum number of iterations.

• Convfactor

Type : int (default: 8)

**Description :** Convergence threshold. If the 2-norm of the residual vector becomes smaller than  $10^{-Convfactor}$ , the calculation finishes.

dyn has the parameters for the computation of the spectrum.

• OmegaMin

**Type :** Complex (default: If invec is not specified, the real part of it becomes the smallest eigenvalue, and the imaginary part of it becomes  $\times 0.01$  times the difference between the largest- and the smallest- eigenvalue. If invec is specified, the default value becomes (0.0, 0.01))

**Description :** The smallest frequency.

• OmegaMax

**Type :** Complex (default: If invec is not specified, the real part of it becomes the largest eigenvalue, and the imaginary part of it becomes  $\times 0.01$  times the difference between the largest- and the smallest- eigenvalue. If invec is specified, the default value becomes (1.0, 0.01))

**Description :** The largest frequency.

• NOmega

Type : int (default: 10)

Description : The number of frequencies.

• outrestart

Type: Logical (default: .FALSE.)

Description : Whether data for restart will be written (.TRUE.) or not (.FALSE.).

• calctype

Type: String. Choose from "normal", "recalc", "restart". (default: "normal")

**Description :** "normal" for computing with the Krylov subspace from scratch. "recalc" for computing with the Krylov subspace generated in the previous calculation. In this case, the matrix-vector product is not performed. The convergence is not guaranteed. "restart" for restarting the calculation from the previous run. In this case, the calculation continues until the convergence is achieved or the number of iteration becomes MaxLoops.

## 5.1.2 "InHam" file

The Hamiltonian is written in the MatrixMarket format.

Example of the "InHam" file:

```
%%MatrixMarket matrix coordinate complex hermitian
16 16 20
1 1 1.000000 0.000000
3 2 0.500000 0.000000
5 3 0.500000 0.000000
6 4 0.500000 0.000000
6 6 -1.000000 0.000000
7 6 0.500000 0.000000
9 2 0.500000 0.000000
9 5 0.500000 0.000000
10 6 0.500000 0.000000
11 4 0.500000 0.000000
11 7 0.500000 0.000000
11 10 0.500000 0.000000
11 11 -1.000000 0.000000
12 8 0.500000 0.000000
13 6 0.500000 0.000000
13 11 0.500000 0.000000
14 12 0.500000 0.000000
15 8 0.500000 0.000000
15 14 0.500000 0.000000
16 16 1.000000 0.000000
```

First row: Arbitrary string (such as comment).

Second row: The number of rows, columns, and non-zero elements (in the lower triangle part).

Third row - End: The row- and the column- index, and the real- and imaginary- part of the non-zero element (in the lower triangle part).

#### 5.1.3 "InVec" file

Right hand side vector is contained.

```
Example of the "InVec" file:
```

```
8192
0.02 0.01
0.02 0.001
(continue...)
```

• First row: [ int01 ]

Type : int

Description : The dimension of the Hilbert space. It must be the same as the dimension of the Hamiltonian.

• Second row - End: [ double01 ] [ double02 ]

Type : double

**Description :** The element of the RHS vector. [double01] is the real part, and [double02] is the imaginary part.

## 5.1.4 Coefficients for restart

The coefficient  $\alpha$  and  $\beta$  are contained.

The name of the generated file is TriDiagComp.dat.

The example of this file:

```
1000

1.0 0.0

0.1 0 0.01 0

0.2 0 0.021 0

(continue...)

2.1 -0.5

3.1 4.0

(continue...)
```

• First row: [ int01 ]

Type : int

**Description :** The length of  $\alpha, \beta$ . It is the same as the number of iterations in the previous run.

• Second row: [ double01 ] [ double02 ]

Type : double

**Description :** The seed frequency  $z_{\text{seed}}$ . [double01] is the real part of  $z_{\text{seed}}$ , and [double02] is the imaginary par of  $z_{\text{seed}}$ .

• Third row - 2 + [ int01 ]th row: [ double03 ] [ double04 ] [ double05 ] [ double06 ]

Type : double

**Description :**  $\alpha, \beta$  at the each iteration. [double03] is the real part of  $\alpha$ , [double04] is the imaginary part of  $\alpha$ , [double05] is the real part of  $\beta$ , [double06] is the imaginary part of  $\beta$ .

• 3 + [ int01 ]th row - 2 + 2  $\times$  [ int01 ]th row: [ double07 ] [ double08 ]

Type : double

**Description :** The product of the RHS vector and the residual vector at the each iteration. [double07] is the real part of it, and [double08] is the imaginary part of it.

#### 5.1.5 Residual vector

The residual vector is contained for the restart. The file name is ResVec.dat.

Example of this file:

```
8192
0.02 0.01
0.02 0.001
(continue...)
0.02 0.01
0.02 0.001
(continue... Only for BiCG)
```

• First row: [ int01 ]

Type : int

**Description :** The dimension of the Hilbert space.

• Second row - 1 + [ int01 ]th row: [ double01 ] [ double02 ]

Type : double

**Description :** Each element of the residual vector. [double01] is the real part of it, and [double02] is the imaginary part of it.

• Third row - 1 + 2 × [ int01 ]th row: [ double03 ] [ double04 ]

Type : double

**Description :** (Only when the Hamiltonian is a complex matrix) Each element of the shadow residual vector. [ double03 ] is the real part of it, [ double04 ] is the imaginary part of it.

## 5.2 Output file

#### 5.2.1 Coefficient for restart

The format is the same as *Coefficients for restart*.

#### 5.2.2 Residual vector

The format is the same as *Residual vector*.

#### 5.2.3 Dynamical Green 's function

The dynamical Green 's function is contained.

Example of this file:

```
-10 0.001 0.001 -0.0001
-9.8 0.001 0.0012 -0.0002
-9.6 0.001 0.0014 -0.0003
(continue...)
```

- First row END: [ double01 ] [ double02 ] [ double03 ] [ double04 ]
  - [ double01 ], [ double02 ]

Type : double

Description : The real- ([ double01 ]) and the imaginary- ([ double02 ]) part of the frequency.

- [ double03 ], [ double04 ]

Type : double

**Description :** The dynamical Green 's function. [double01] is the real part of it, and [double02] is the imaginary part of it.

# CONTACT

If you have any comments, questions, bug reports etc. about this program, please contact to the main developer (Mitsuaki Kawamura) by sending the e-mail (the address is shown below).

mkawamura\_at\_issp.u-tokyo.ac.jp

Please change  $\_at\_$  into @, when you will send the e-mail.